











Algebra Tiles

Introduction

Algebra tiles are hands-on maths manipulatives used to visualise algebraic expressions and equations. Each tile is double-sided and features two colours. The blue/green/yellow side represents a positive value, and the red side represents the negative values.

There are three different size tiles.

- The small squares or unit tiles  +1 or  -1
- The rectangular tiles or variable tiles  +X or  -X
- The large squares or X^2 tiles  + X^2 or  - X^2

By placing a positive tile directly next to its corresponding negative tile creates a 'zero pair' as they cancel each other out. For example,  +  = 0. Together they equal zero and by removing the cancelled out zero pairs will help to see exactly what the variable equals.

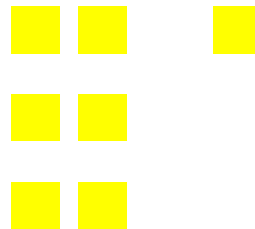
Starting Activities: Algebraic Substitution

Example 1: Find $3x + 1$ if $x = 2$

STEP 1: Model the expression $3x + 1$ with the tiles



STEP 2: Using the information $x=2$, substitute each x tile for two 1 tiles.



Now it is easy to see that if $x=2$ then $3x + 1 = 7$

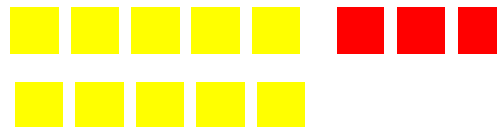
Starting Activities: Algebraic Substitution

Example 2: Find $2x - 3$ if $x = 5$

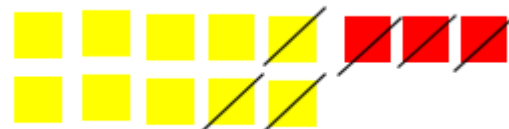
STEP 1: Model the expression $2x - 3$ with the tiles.



STEP 2: Using the information $x=5$, substitute each x tile for five 1 tiles.



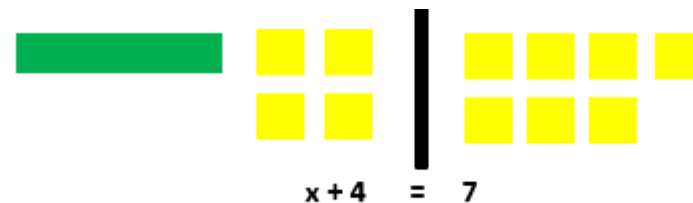
STEP 3: Each red tile cancels out a yellow tile because they are additive inverses. So, if $x = 5$ then $2x - 3 = 7$



Moving On: Solving Equations

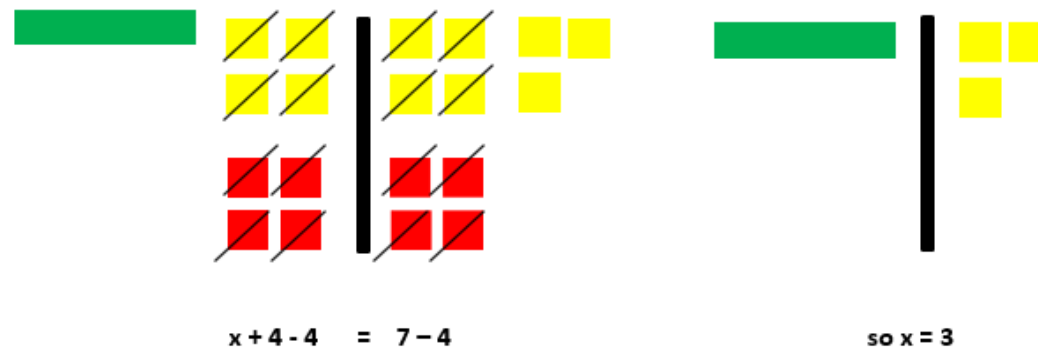
Example 1: $x + 4 = 7$

STEP 1: Model the equation using the tiles. You will need a defined space for each side of the equation.



STEP 2: We need to isolate the variable tiles (x) to find their value.

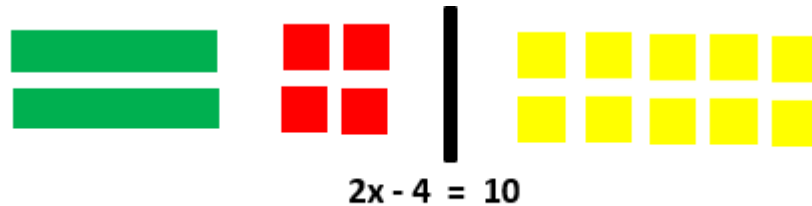
To do this we create additive inverse pairs. Each of the four '+1' tiles from the left can be paired with the four '-1' tiles to create 0 pairs, thus removing them from the calculation. Both sides of the equation maintain equality.



Moving On: Solving Equations

Example 2: $2x - 4 = 10$

STEP 1: Model the equation using the tiles. You will need a defined space for each side of the equation.



Moving On: Solving Equations

STEP 2: We need to isolate the variable tiles (x) to find their value.

To do this we create additive inverse pairs. Each of the four '-1' tiles from the left, pair them with 4 '+1' tiles, thus removing them from the calculation, then add four '+1' tiles to the right to maintain equality.

$$2x - 4 + 4 = 10 + 4$$

$$\text{So } 2x = 14$$

$$\text{So } x = 7$$